

BHARATHIAR UNIVERSITY, COIMBATORE.
M. Sc. MATHEMATICS DEGREE COURSE (AFFILIATED COLLEGES)
(Effective from the academic Year 2015-2016)
SCHEME OF EXAMINATIONS – CBCS PATTERN

Sem.	Study Components	Course title	Ins. hrs/ week	Examinations				Credit
				Dur:Hrs	CIA	Marks	Total Marks	
I	Paper 1	Algebra	7	3	25	75	100	4
	Paper 2	Real Analysis	7	3	25	75	100	4
	Paper 3	Ordinary Differential Equations	6	3	25	75	100	4
	Paper 4	Numerical Methods	6	3	25	75	100	4
	Elect. Paper I		4	3	25	75	100	4
II	Paper 5	Complex Analysis	6	3	25	75	100	4
	Paper 6	Partial Differential Equations	7	3	25	75	100	4
	Paper 7	Mechanics	7	3	25	75	100	4
	Paper 8	Operations Research	6	3	25	75	100	4
	Elect. Paper II		4	3	25	75	100	4
III	Paper 9	Topology	7	3	25	75	100	4
	Paper 10	Fluid Dynamics	7	3	25	75	100	4
	Paper 11	Mathematical Statistics	6	3	25	75	100	4
	Paper 12	Graph Theory	6	3	25	75	100	4
	Elect. Paper III		4	3	25	75	100	4
IV	Paper 13	Functional Analysis	7	3	25	75	100	4
	Paper 14	Mathematical Methods	7	3	25	75	100	4
	Paper 15	Computer Programming (C++ Theory)	4	3	25	75	100	4
	Practical	Computer Programming (C++ Practical)	2	3	40	60	100	4
	Paper 16	Number Theory	6	3	25	75	100	4
	Elect. Paper IV		4	3	25	75	100	4
	Project						150*	6
Total							2250	90

* For Project report – 120 marks, Viva-voce – 30 marks.

LIST OF ELECTIVES

- | | |
|--|-------------------------------------|
| 1.Mathematical Softwares**
(<i>LaTex, MATLAB and Mathematica</i>) | 5.Fuzzy Logic and Fuzzy Sets |
| 2.Magnetohydro Dynamics | 6.Cryptography |
| 3.Control Theory | 7. Neural Networks |
| 4.Differential Geometry | 8.Stochastic Differential Equations |

Note : The syllabus for all the above papers (except Paper XIV – Mathematical Methods & Elective paper Mathematical Softwares) be the same as prescribed for the academic year 2014-15. The syllabus for the Paper XIV – Mathematical Methods, Elective paper Mathematical Softwares are furnished below. For Paper IV – Numerical Methods one more reference book is added.

** Theory – 2 hrs – 75 Marks (20 CIA +55 External)
Practical – 2 hrs – 25 Marks (10 CIA +15 External)

PAPER IV: NUMERICAL METHODS

Unit I:

SOLUTION OF NONLINEAR EQUATIONS:

Newton's method – Convergence of Newton's method – Bairstow's Method for quadratic factors
NUMERICAL DIFFERENTIATION AND INTEGRATION: Derivatives from Differences tables – Higher order derivatives – Divided difference, Central-Difference formulas – Composite formula of Trapezoidal rule – Romberg integration – Simpson's rules.

Unit II:

SOLUTION OF SYSTEM OF EQUATIONS:

The Elimination method – Gauss and Gauss Jordan methods – LU Decomposition method – Matrix inversion by Gauss-Jordan method – Methods of Iteration – Jacobi and Gauss Seidal Iteration – Relaxation method – Systems of Nonlinear equations.

Unit III:

SOLUTION OF ORDINARY DIFFERENTIAL EQUATIONS:

Taylor series method – Euler and Modified Euler methods – Rungekutta methods – Multistep methods – Milne's method – Adams Moulton method.

Unit IV:

BOUNDARY VALUE PROBLEMS AND CHARACTERISTIC VALUE PROBLEMS: The shooting method – solution through a set of equations – Derivative boundary conditions – Characteristic value problems – Eigen values of a matrix by Iteration – The power method.

Unit V:

NUMERICAL SOLUTION OF PARTIAL DIFFERENTIAL EQUATIONS:

(Solutions of Elliptic, Parabolic and Hyperbolic partial differential equations)
Representation as a difference equation – Laplace's equation on a rectangular region – Iterative methods for Laplace equation – The Poisson equation – Derivative boundary conditions – Solving the equation for time-dependent heat flow (i) The Explicit method (ii) The Crank Nicolson method – solving the wave equation by Finite Differences.

Treatment as in:

1. APPLIED NUMERICAL ANALYSIS' by C.F.Gerald and P.O.Wheatley, Fifth Edition, Addison Wesley, (1998).

Reference Book:

1. S.C. Chapra and P.C. Raymond: Numerical Methods for Engineers, tata McGraw Hill, New Delhi, (2000)
2. R.L. Burden and J. Douglas Faires: Numerical Analysis, P.W.S.Kent Publishing Company, Boston (1989), Fourth Edition.
3. S.S. Sastry: Introductory methods of Numerical Analysis, Prentice Hall of India, New Delhi, (1998).
4. P.Kandasamy et al., Numerical Methods, S.Chand & Co.Ltd., New Delhi(2003)

PAPER XIV: MATHEMATICAL METHODS

Unit I:

FOURIER TRANSFORMS: Fourier sine and cosine transforms – Fourier transforms of derivatives - Fourier transforms of simple functions - convolution integral – Parseval’s Theorem - Solution of PDE by Fourier transform – Laplace equation in half plane in infinite strips; in semi infinite strip. The Linear diffusion equation on a semi infinite line – the two dimensional diffusion equation.

Unit II:

HANKEL TRANSFORMS: Properties of Hankel Transforms – Hankel transformation of derivatives of functions – Hankel Inversion Theorem (Statement only)- The Parseval’s relation – relation between Fourier and Hankel transforms - Axisymmetric Dirichlet problem for a half space - Axisymmetric Dirichlet problem for a thick plate.

Unit III:

INTEGRAL EQUATIONS: Types of Integral equations – Integral Fredholm Alternative - Approximate method – Equation with separable Kernel - Volterra integral equations – Fredholm’s theory – Fredholm’s first, second, third theorems.

Unit IV:

Application of Integral equation to ordinary differential equation – initial value problems – Boundary value problems – singular integral equations – Abel Integral equation

Unit V:

CALCULUS OF VARIATIONS: Variation and its properties – Euler’s equation – Functionals of the integral forms - Functional dependent on higher order derivatives – functionals dependent on the functions of several independent variables – variational problems in parametric form –applications.

Treatment as in: For Units I and II:

The Use of Integral Transforms by I.N.Sneddon, Tata Mc Graw Hill, New Delhi, 1974.

For Units III and IV:

Linear Integral Equations Theory and Technique by R.P.Kanwal, Academic Press, New York, 1971.

For Unit V:

Differential Equations and Calculus of Variations by L.Elsgolts, Mir Publishers, Moscow, 1970.

Unit I	:	Chapter 2:	2.4 - 2.7, 2.9 – 2.10, 2.16 – 2-(a).(b).(c) 2.16.
Unit II	:	Chapter 5:	5.2 – 5.4, 5.6 – 5.7, 5.10 – 5.12.
Unit III	:	Chapter 2:	2.3 - 2.5, Chapter 3: 3.3 - 3.4.
Unit IV	:	Chapter 5:	5.1 – 5.2, Chapter 8: 8.1 – 8.2.
Unit V	:	Chapter 6:	6.1 – 6.7.

Elective Paper –I
Mathematical Softwares (LaTeX, MATLAB and Mathematica)

Unit I: Basis of a LaTeX file – Special Characters, Document layout and organization – Document Class, Page Style, Parts of the Document, Centering and Indenting, List, Theorem-Like Declarations, Boxes, Tables.

Unit II: Foot notes and Marginal notes, Mathematical formulas – Mathematical Environments, Main elements of math mode, Mathematical Symbols, Additional Elements, Fine Tuning Mathematics, Drawing Pictures with LaTeX.

Unit III: MATLAB Windows – Online help – Matrices and Vectors – Matrix and Array Operations – Inline functions – Function files.

Unit IV: Loops – Linear Algebra – Data Analysis and Statistics – Ordinary Differential Equations – Nonlinear Algebraic Equations – Basic 2D and 3D Plot (Syntax only).

Unit V: Mathematica Commands (General form, Example, Uses only):
Calculus: **Limit**[f[x], x→a] - **D**[f[x], x] - **D**[f[x],{x, n}] . Differential
Integral Calculus:
Integrate [f[x], x] - **Integrate**[f[x],{x, a, b}] - **NIntegrate**[f[x],{x, a, b}] . Partial Derivatives:
D[f,x] – **D**[f,{x,n}] . - Total Differential: **Dt**[f[x, y]] - **Dt**[f[x, y],x] .
Multiple Integrals:**Integrate**[f[x,y],{x,a,b},{y,c,d}]. Differential Equations: **DSolve**[eqn,y[x],x] –
NDSolve[eqn,y,{x,xmin,xmax}] . Algebra: **Expand** [] - **Factor** [] - **Roots** [] - **Solve**[eqn,var].
Matrices: **Determinant**[mx] - **Inverse**[mx] - **Eigenvalues**[mx]- **Eigenvectors**[mx] .
Graphics: **Plot**[f[x],{x,a,b}] – **Plot**[f[x],g[x],{x,a,b}] – **ParametricPlot**[{x[t],y[t],{t,a,b}] -
Plot3D[{f[x,y],{x,a,b},{y,c,d}}].

Text Books:

1) **H. Kopka and P.W. Daly**, “A Guide to LATEX”, Third Edition, Addison – Wesley, London, 1999.

Unit I: Chapter 2: Sections: 2.5, Chapter 3: Sections: 3.1 – 3.3, Chapter 4: Sections: 4.2, 4.3, 4.5, 4.7, 4.8

Unit II: Chapter 4: Sections: 4.10, Chapter 5: Sections: 5.1 – 5.5, Chapter 6: Sections: 6.1.

2) **Rudra Pratap**, “Getting Started with MATLAB” Indian Edition, Oxford University Press.

Unit III: Chapter 1: Sections: 1.6.1, 1.6.2, Chapter 3: Sections: 3.1, 3.2, 3.5.1, Chapter 4: Sections: 4.2, 4.2.1.

Unit IV: Chapter 4: Sections: 4.3.4, Chapter 5: Sections: 5.1, 5.3, 5.5, 5.6, Chapter 6: Sections: 6.1, 6.3.

3) **Eugene Don, Ph.D.** Mathematica (schaum’s outlines) ,Mc.Graw.Hill.

Unit V

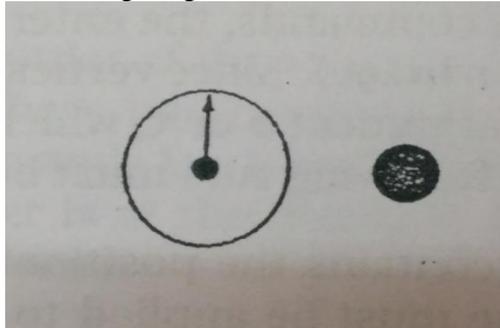
Mathematical Softwares (LaTeX, MATLAB and Mathematica)

Practical List of Programs

1. (a) Using LaTeX, type the following paragraph, to including the 9.5in text height, 6.30in text width, 0.10in left margin, 0.120in right margin, -0.6in top margin, 1.5in line space and foot notes.
 - (b) Write the MATLAB program to generate Fibonacci series.
 - (c) Using MATHEMATICA to compute the area bounded by the curves $f(x) = 1-x^2$ and $g(x) = x^4-3x^2$. [Q: 9.8]
2. (a) Using LaTeX, type the following formula

$$a_0 + \frac{1}{a_1 + \frac{1}{a_2 + \frac{1}{a_3 + \frac{1}{a_4}}}} + \begin{pmatrix} a & b \\ c & d \end{pmatrix} + \sum_{\alpha=0}^{\infty} (\beta^\alpha + \Gamma^\alpha)$$

- (b) Using MATLAB, Solve the following system of equations by matrix method $2x+y = 13, x-3y = -18$.
 - (c) Using MATHEMATICA, sketch the Sphere $x^2+y^2+z^2=14$ and its tangent plane at the point (1,2,3). [Q: 10.7]
3. (a) Using LaTeX, draw the following diagram:



- (b) Using MATLAB, solve the following first order linear differential equation using Euler method: $\frac{dy}{dx} = -y, y(0)=1$. Draw the graph and compare the exact solution.
 - (c) Using MATHEMATICA, plot the (five) solutions for : $d^2y/dx^2+0.3 dy/dx+\sin y=0$ with $0 \leq x \leq 30$ and using initial conditions $y'(0)=0, y(0)= -2,-1,0,1$ and 2 . [Q: 11.17]
4. (a) Create the following table using LaTeX:

S.No.	Register Number	Name of the Student	Percentage of Marks	Rank
1	xxxxxxx	xxxxxxx	xxxxx	xxxx
2	xxxxxxx	xxxxxxx	xxxxx	xxxx
3	xxxxxxx	xxxxxxx	xxxxx	xxxxx

(b) Calculate mean, median, standard deviation, variance, maximum value, minimum value, range, skewness and kurtosis for the following data:

40 41 45 49 50 51 55 59 60 60

(c) Using MATHEMATICA, solve the differential equation $\frac{dy}{dx}=1+\frac{1}{2}y^2$, $y(0)=1$, $0 \leq x \leq 1$, with **DSolve** and **NDSolve** and compare the results. [Q: 11.15]